## Basic Techniques for Single-Figure Tessellations

A tiling of an object is a pattern of figures that fills the object with no overlaps and no gaps. Tessellations usually refer to tilings of a plane by repeatedly tracing a single geometric object.

- The word "tessella" means "small square" (derived from "tessera", the Greek word for "four"). That lines up nicely with what we picture when we say "tiling."
- It's generally good to construct a tessellation shape out of sturdy material. It also helps to mark the edges (e.g., with different colors).
- The examples show single edge-modifications, but you can modify multiple edges to get more interesting shapes.


## Simple Translation Tessellation

Polygon should have opposite sides that are parallel and congruent (e.g., squares, parallelograms, regular hexagons).


Start with a square


Draw a design on one side of the square.


Cut the design piece out and slide (translation) it across to the opposite side of the square.


Tape the cutout piece to the opposite side of the square to compl ete the pattern (tile). Slide (translation) the pattern when tracing.

## Glide Reflection Tessellation

Polygon should have opposite sides that are parallel and congruent (e.g., squares, parallelograms, regular hexagons).


Start with a square.


Draw a design on one side of the square.


Cut the design piece out and slide (translation) it across to the opposite side of the square. Flip (reflect) the cut piece on its vertical axis.


Tape the cutout piece to the opposite side of the square to complete the pattern. This pattern (tile) needs to be rotated or flipped as it is traced

## Side-Rotation Tessellation

Adjacent sides must be congruent (e.g., squares, equilateral triangles, regular hexagons, parallelograms). The central angle must divide 360 degrees.


Starf with a square.


Draw a design on one side of the square.


Cut the design piece out and tum (rotate) it on an end point until it lies evenly with an adjacent side of the square.


Tape the cutout piece to the adjacent side of the square to complete the pattem. This pattern (tile) needs to be rotated as it is traced.

## Midpoint-Rotation Tesselation

The underlying pattern must tesselate the plane (e.g., triangles, squares, quadrilaterals, regular hexagons)


Start with a square.


Draw a design "nibble" from one comer to the midpoint of a side of a square.


Cut the design piece out and tum (rotate) the "nibble" about the side's midpoint onfo the remaining half of of the square. (uncut portion, same side)


Tape the cutout piece to the uncut half of the same side of the square to complete the pattem. This pattem (tile) needs to be rotated as it is traced.

## Arbitrary Quadrilateral Tesselation

Begin with an arbitrary quadrilateral ABCD. Rotate by $180^{\circ}$ about the midpoint of one of its sides, and then repeat using the midpoints of other sides to build up a tessellation.


